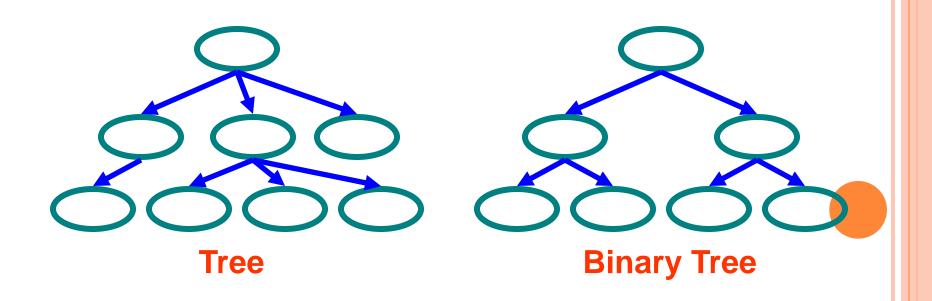
TREE DATA STRUCTURES

TREES DATA STRUCTURES • Tree

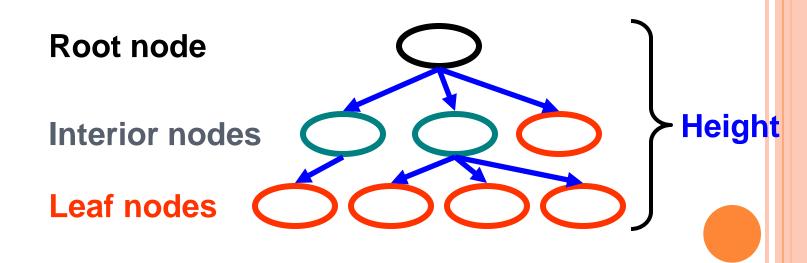
- Nodes
- Each node can have 0 or more children
- A node can have at most one parent
- Binary tree
 - Tree with 0–2 children per node



TREES

Terminology

- Root ⇒ no parent
- Leaf \Rightarrow no child
- Interior \Rightarrow non-leaf
- Height ⇒ distance from root to leaf



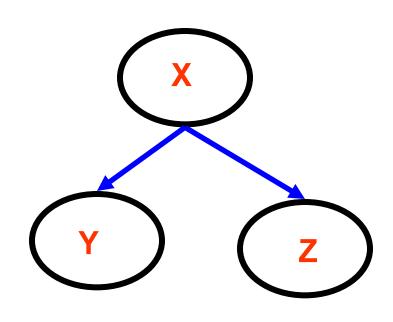
BINARY SEARCH TREES

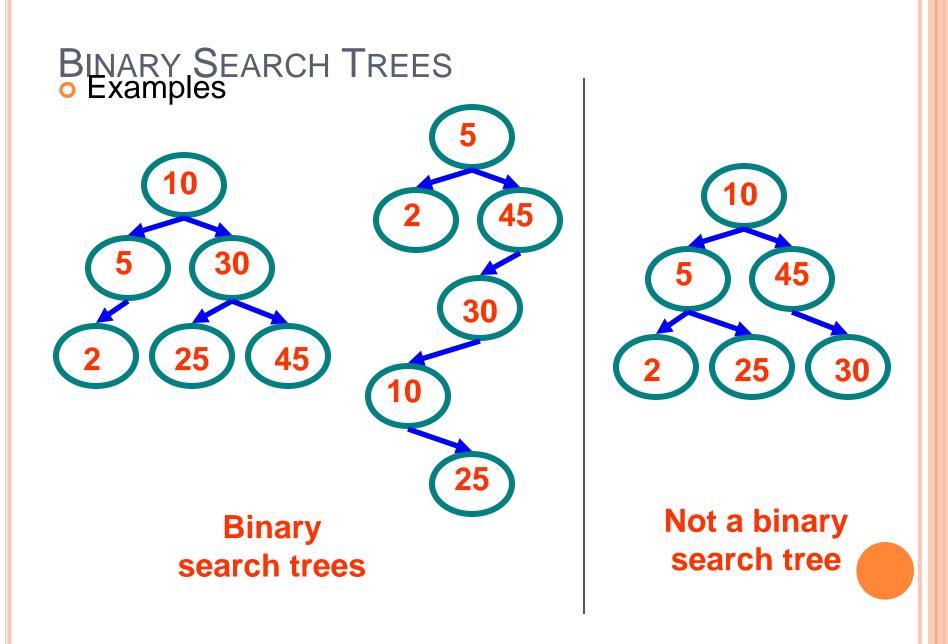
Key property

- Value at node
 - Smaller values in left subtree
 - Larger values in right subtree
- Example

• X > Y

• X < Z





BINARY TREE IMPLEMENTATION

```
Class Node {
```

int data; // Could be int, a class, etc Node *left, *right; // null if empty

```
void insert ( int data ) { ... }
void delete ( int data ) { ... }
Node *find ( int data ) { ... }
```

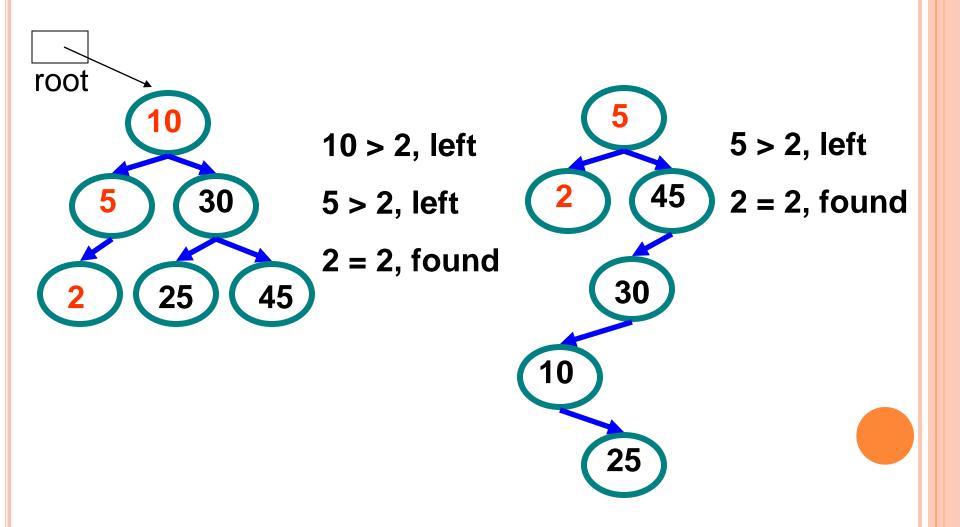
```
ITERATIVE SEARCH OF BINARY TREE
Node *Find( Node *n, int key) {
   while (n != NULL) {
   if (n->data == key) // Found it
         return n;
      if (n->data > key)
                                  // In left subtree
         n = n -> left;
                                  // In right subtree
      else
         n = n - right;
    return null;
Node * n = Find(root, 5);
```

RECURSIVE SEARCH OF BINARY TREE

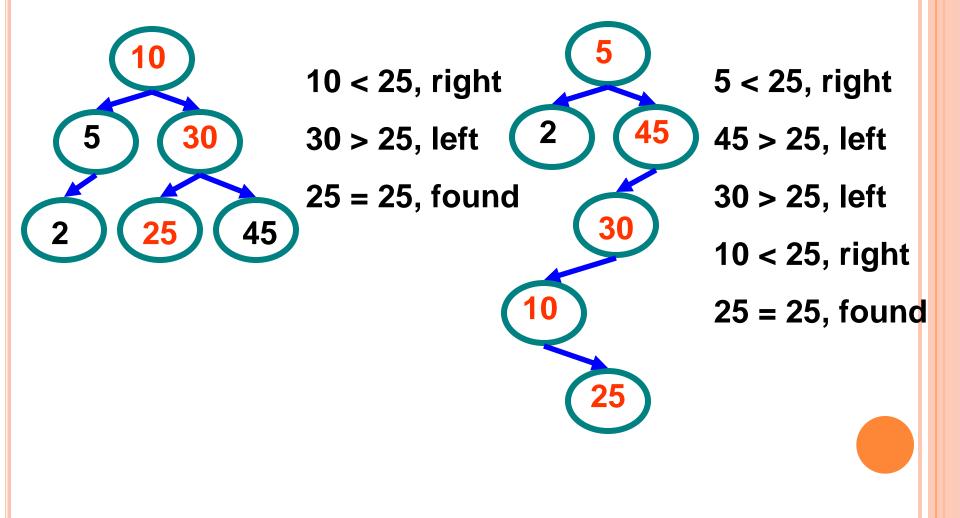
```
Node *Find( Node *n, int key) {
   if (n == NULL) // Not found
      return( n );
   else if (n->data == key) // Found it
      return(n);
   else if (n->data > key) // In left subtree
      return Find( n->left, key );
                                  // In right subtree
    else
      return Find( n->right, key );
```

```
Node * n = Find(root, 5);
```

EXAMPLE BINARY SEARCHES • Find (root, 2)

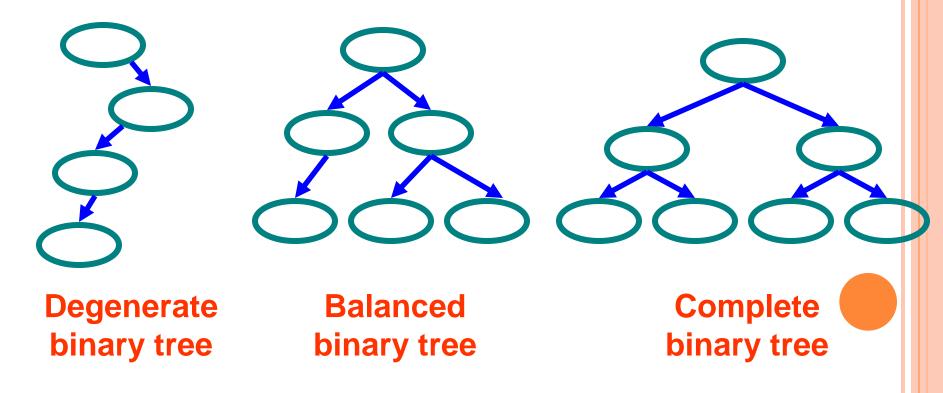


EXAMPLE BINARY SEARCHES • Find (root, 25)



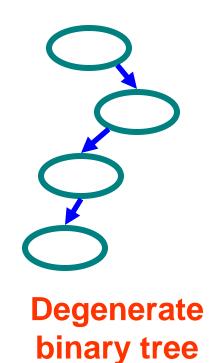
TYPES OF BINARY TREES Degenerate – only one child

- Complete always two children
- Balanced "mostly" two children
 - more formal definitions exist, above are intuitive ideas

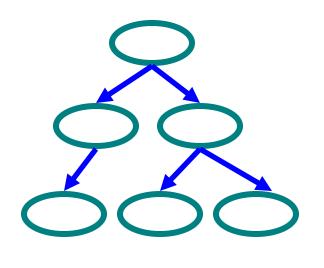


BINARY TREES PROPERTIES Balanced

- Height = O(n) for n nodes
- Similar to linked list



- Height = O(log(n)) for n nodes
- Useful for searches



Balanced binary tree

BINARY SEARCH PROPERTIES

Time of search

- Proportional to height of tree
- Balanced binary tree
 O(log(n)) time
- Degenerate tree
 - o O(n) time
 - Like searching linked list / unsorted array

BINARY SEARCH TREE CONSTRUCTION

- How to build & maintain binary trees?
 - Insertion
 - Deletion
- Maintain key property (invariant)
 - Smaller values in left subtree
 - Larger values in right subtree

BINARY SEARCH TREE - INSERTION

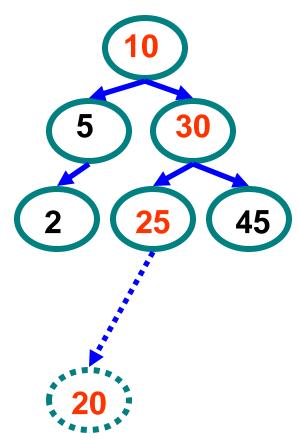
- Algorithm
 - 1. Perform search for value X
 - 2. Search will end at node Y (if X not in tree)
 - 3. If X < Y, insert new leaf X as new left subtree for Y
 - 4. If X > Y, insert new leaf X as new right subtree for Y

Observations

- O(log(n)) operation for balanced tree
- Insertions may unbalance tree

EXAMPLE INSERTION

o Insert (20)



10 < 20, right

30 > 20, left

25 > 20, left

Insert 20 on left

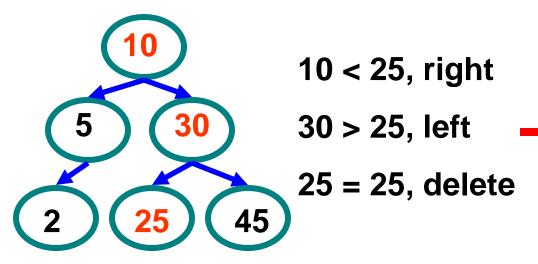
BINARY SEARCH TREE – DELETION

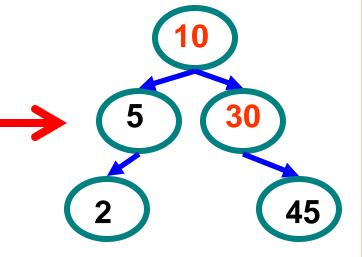
- o Algorithm
 - 1. Perform search for value X
 - 2. If X is a leaf, delete X
 - 3. Else // must delete internal node

 a) Replace with largest value Y on left subtree
 OR smallest value Z on right subtree
 b) Delete replacement value (Y or Z) from subtree
- Observation
 - O(log(n)) operation for balanced tree
 - Deletions may unbalance tree

EXAMPLE DELETION (LEAF)

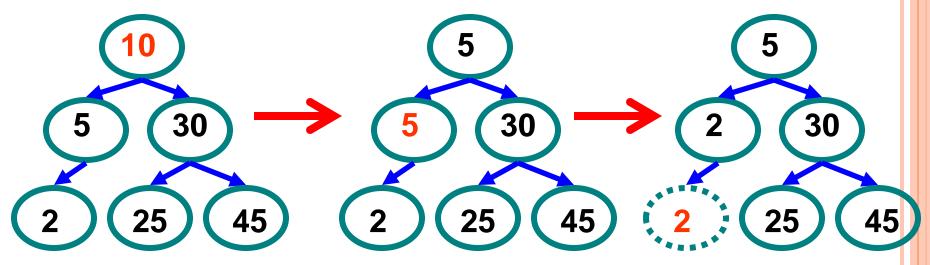
o Delete (25)





EXAMPLE DELETION (INTERNAL NODE)

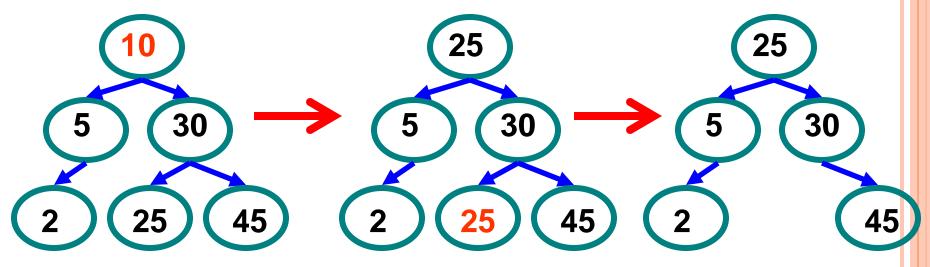
o Delete (10)



Replacing 10 with largest value in left subtree Replacing 5 with largest value in left subtree **Deleting leaf**

EXAMPLE DELETION (INTERNAL NODE)

o Delete (10)



Deleting leaf

Resulting tree

Replacing 10 with smallest value in right subtree

BALANCED SEARCH TREES

Kinds of balanced binary search trees

- height balanced vs. weight balanced
- "Tree rotations" used to maintain balance on insert/delete

Non-binary search trees

- 2/3 trees
 - o each internal node has 2 or 3 children
 - o all leaves at same depth (height balanced)
- B-trees
 - Generalization of 2/3 trees
 - Each internal node has between k/2 and k children
 - Each node has an array of pointers to children
 - Widely used in databases

OTHER (NON-SEARCH) TREES

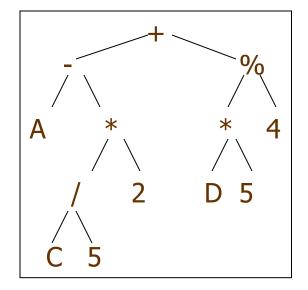
Parse trees

- Convert from textual representation to tree representation
- Textual program to tree
 Used extensively in compilers
- Tree representation of data
 - E.g. HTML data can be represented as a tree
 - called DOM (Document Object Model) tree
 - o XML
 - Like HTML, but used to represent data
 - Tree structured

PARSE TREES

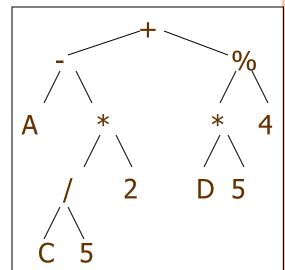
 Expressions, programs, etc can be represented by tree structures

- E.g. Arithmetic Expression Tree
- A-(C/5 * 2) + (D*5 % 4)



TREE TRAVERSAL

Goal: visit every node of a tree
in-order traversal



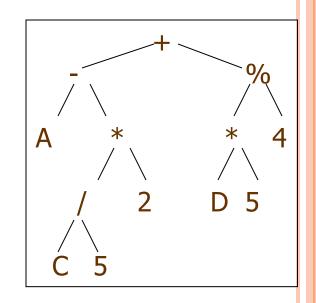
```
void Node::inOrder () {
    if (left != NULL) {
        cout << ``(``; left->inOrder(); cout << ``)'';
    }
    cout << data << endl;
    if (right != NULL) right->inOrder()

Output: A - C / 5 * 2 + D * 5 % 4
To disambiguate: print brackets
```

TREE TRAVERSAL (CONTD.)

o pre-order and post-order:

```
void Node::preOrder () {
   cout << data << endl;
   if (left != NULL) left->preOrder ();
   if (right != NULL) right->preOrder ();
}
```



Output: + - A * / C 5 2 % * D 5 4

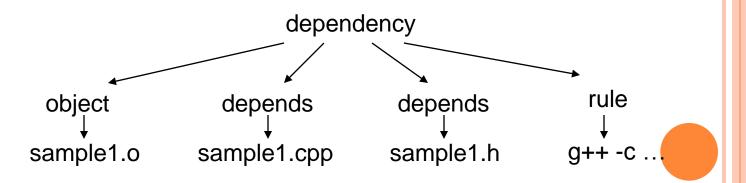
```
void Node::postOrder () {
    if (left != NULL) left->preOrder ();
    if (right != NULL) right->preOrder ();
    cout << data << endl;
}
Output: A C 5 / 2 * - D 5 * 4 % +</pre>
```

Obata Representation

• E.g.

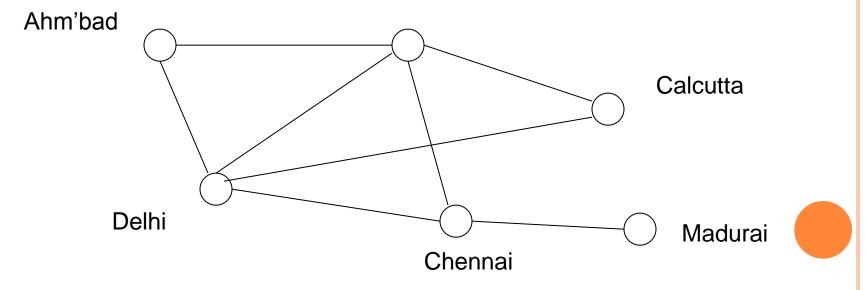
<dependency> <object>sample1.o</object> <depends>sample1.cpp</depends> <depends>sample1.h</depends> <rule>g++ -c sample1.cpp</rule> </dependency>

Tree representation



GRAPH DATA STRUCTURES

- E.g: Airline networks, road networks, electrical circuits
- o Nodes and Edges
- E.g. representation: class Node
 - Stores name
 - stores pointers to all adjacent nodes
 - i,e. edge == pointer
 - To store multiple pointers: use array or linked list Mumbai



END OF CHAPTER